

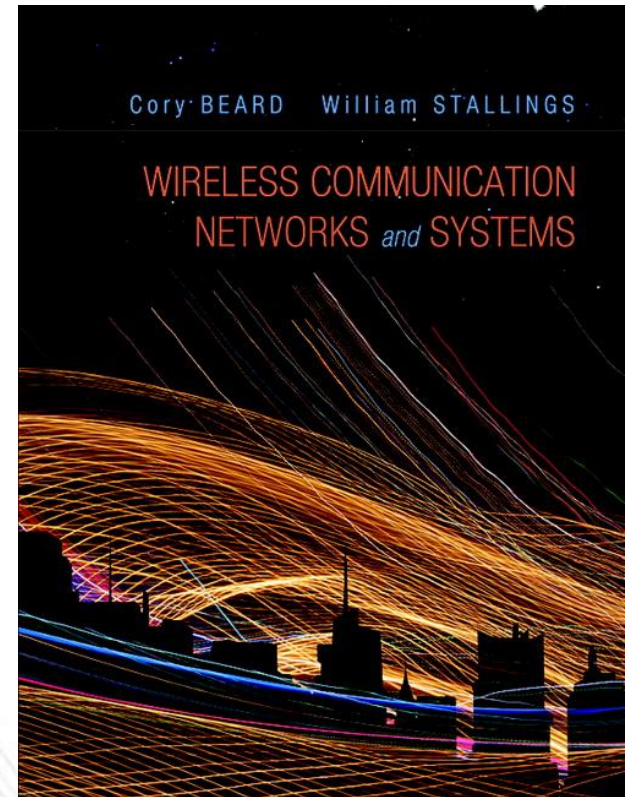
# CHAPTER 8 ORTHOGONAL FREQUENCY DIVISION MULTIPLEXING (OFDM)

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## **Wireless Communication Networks and Systems**

1<sup>st</sup> edition

**Cory Beard, William Stallings**

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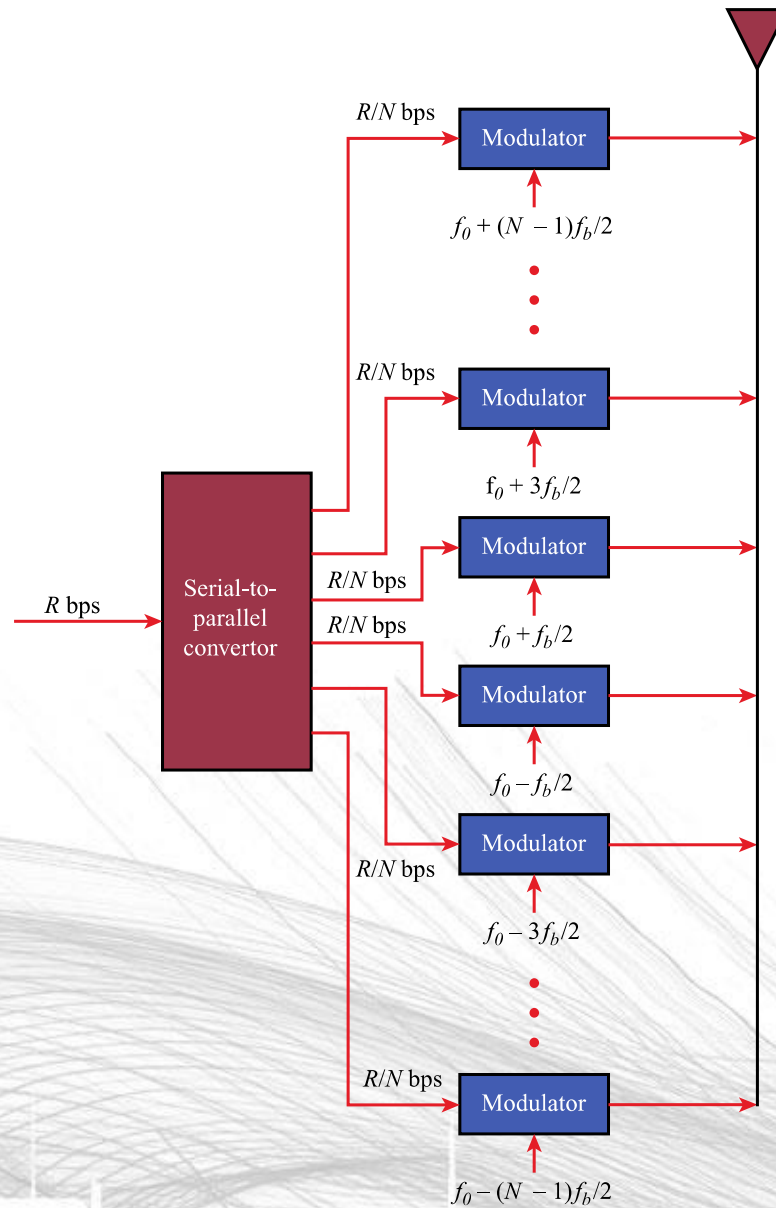
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# INTRODUCTION

- OFDM created great expansion in wireless networks
  - Greater efficiency in bps/Hz
- Main air interface in the change from 3G to 4G
  - Also expanded 802.11 rates
- Critical technology for broadband wireless access
  - WiMAX

# HOW OFDM WORKS

- Also called multicarrier modulation
- Start with a data stream of  $R$  bps
  - Could be sent with bandwidth  $Nf_b$
  - With bit duration  $1/R$
- OFDM splits into  $N$  parallel data streams
  - Called *subcarriers*
  - Each with bandwidth  $f_b$
  - And data rate  $R/N$  (bit time  $N/R$ )

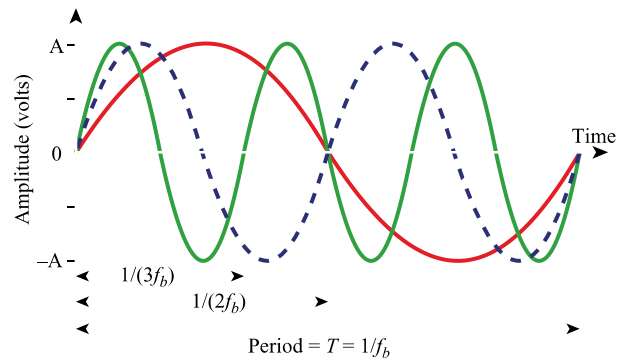


**FIGURE 8.1 CONCEPTUAL UNDERSTANDING OF ORTHOGONAL FREQUENCY DIVISION MULTIPLEXING**

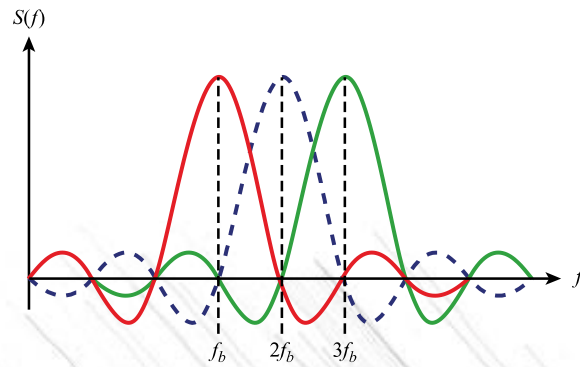


# ORTHOGONALITY

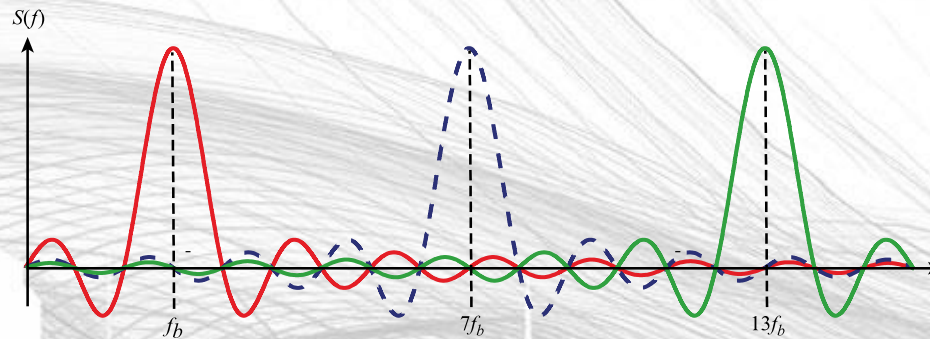
- The spacing of the  $f_b$  frequencies allows tight packing of signals
  - Actually with overlap between the signals
  - Signals at spacing of  $f_b, 2f_b, 3f_b$ , etc.
- The choice of  $f_b$  is related to the modulation symbol rate to make the signals *orthogonal*
  - Average over symbol time of  $s_1(t) \times s_2(t) = 0$
  - Receiver is able to extract only the  $s_1(t)$  signal
    - If there is no corruption in the frequency spacing
- Traditional FDM makes signals completely avoid frequency overlap
  - OFDM allows overlap which greatly increases capacity



(a) Three subcarriers in time domain



(b) Three orthogonal subcarriers in frequency domain



(c) Three carriers using traditional FDM

## FIGURE 8.2 ILLUSTRATION OF ORTHOGONALITY OF OFDM



# ORTHOGONALITY

- Given an OFDM subcarrier symbol time of  $T$ 
  - $f_b$  must be a multiple of  $1/T$
- Example: IEEE 802.11n wireless LAN
  - 20 MHz total bandwidth
    - Only 15 MHz can be used
  - 48 subcarriers
  - $f_b = 0.3125$  MHz
  - Signal is translated to 2.4 GHz or 5 GHz bands

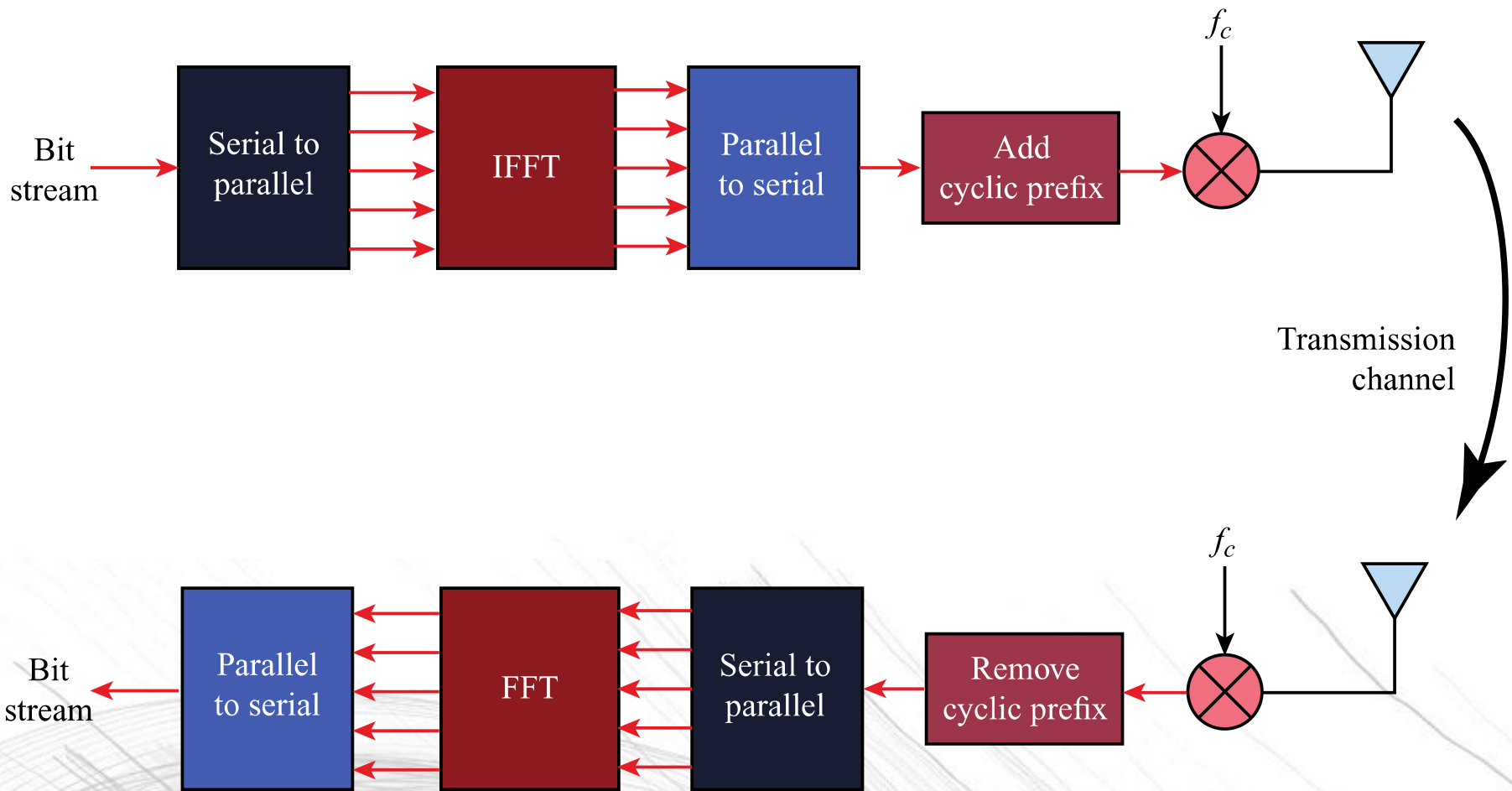
# BENEFITS OF OFDM

- Frequency selective fading only affects some subcarriers
  - Can easily be handled with a forward error-correcting code
- More importantly, OFDM overcomes intersymbol interference (ISI)
  - ISI is caused by multipath signals arriving in later bits
  - OFDM bit times are much, much longer (by a factor of  $N$ )
    - ISI is dramatically reduced
  - $N$  is chosen so the root-mean-square delay spread is significantly smaller than the OFDM bit time
  - It may not be necessary to deploy equalizers to overcome ISI
    - Eliminates the use of these complex and expensive devices.



# OFDM IMPLEMENTATION

- Inverse Fast Fourier Transform (IFFT)
  - The OFDM concept (Figure 8.1) would use  $N$  oscillators for  $N$  different subcarrier frequencies
    - Expensive for transmitter and receiver
  - Discrete Fourier Transform (DFT) processes digital signals
    - If  $N$  is a power of two, the computational speed dramatically improves by using the fast version of the DFT (FFT).
  - Transmitter takes a symbol from each subcarrier
    - Makes an *OFDM symbol*
    - Uses the Inverse FFT to compute the data stream to be transmitted
    - OFDM symbol provides the weights for each subcarrier
    - Then it is sent on the carrier using only one oscillator



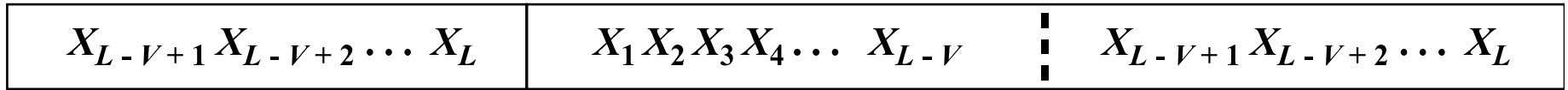
FFT = fast Fourier transform  
 IFFT = inverse fast Fourier transform

**FIGURE 8.3 IFFT IMPLEMENTATION OF OFDM**



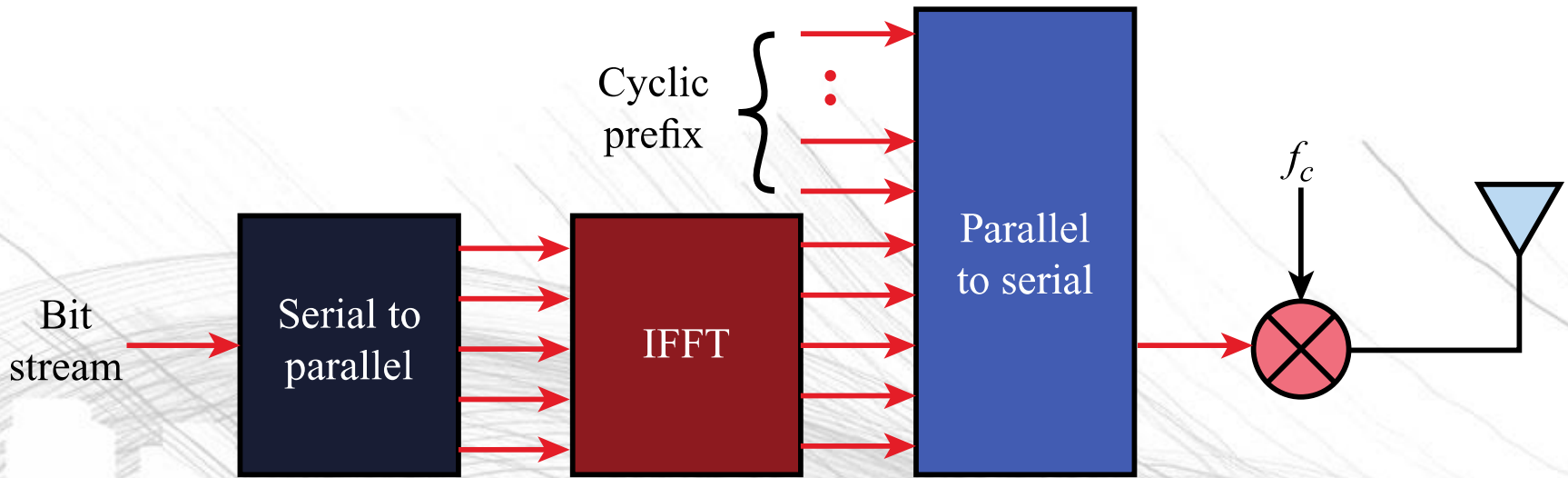
# CYCLIC PREFIX

- OFDM's long bit times eliminate most of the ISI
- OFDM also uses a *cyclic prefix* (CP) to overcome the residual ISI
  - Adds additional time to the OFDM symbol before the real data is sent
    - Called the *guard interval*
    - ISI diminishes before the data starts
  - Data from the end of the OFDM symbol is used as the CP
    - Simplifies the computations



Copy the last  $V$  samples

**(a) OFDM Symbol Format**



**(b) OFDM Block Diagram Showing Cyclic Prefix**

**FIGURE 8.4 CYCLIC PREFIX**

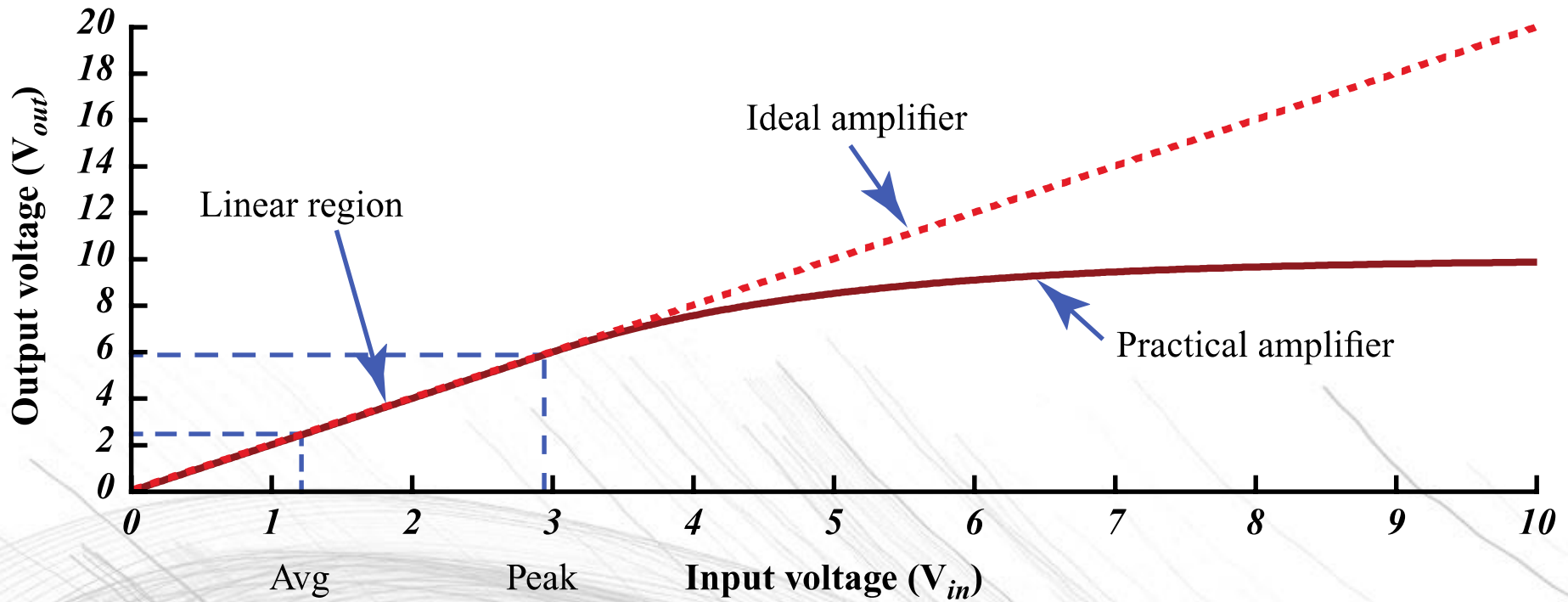


# DIFFICULTIES OF OFDM

- Peak-to-average power ratio (PAPR)
  - For OFDM signals, this ratio is much higher than for single-carrier signals
  - OFDM signal is a sum of many subcarrier signals
    - Total can be very high or very low
- Power amplifiers need to amplify all amplitudes equally

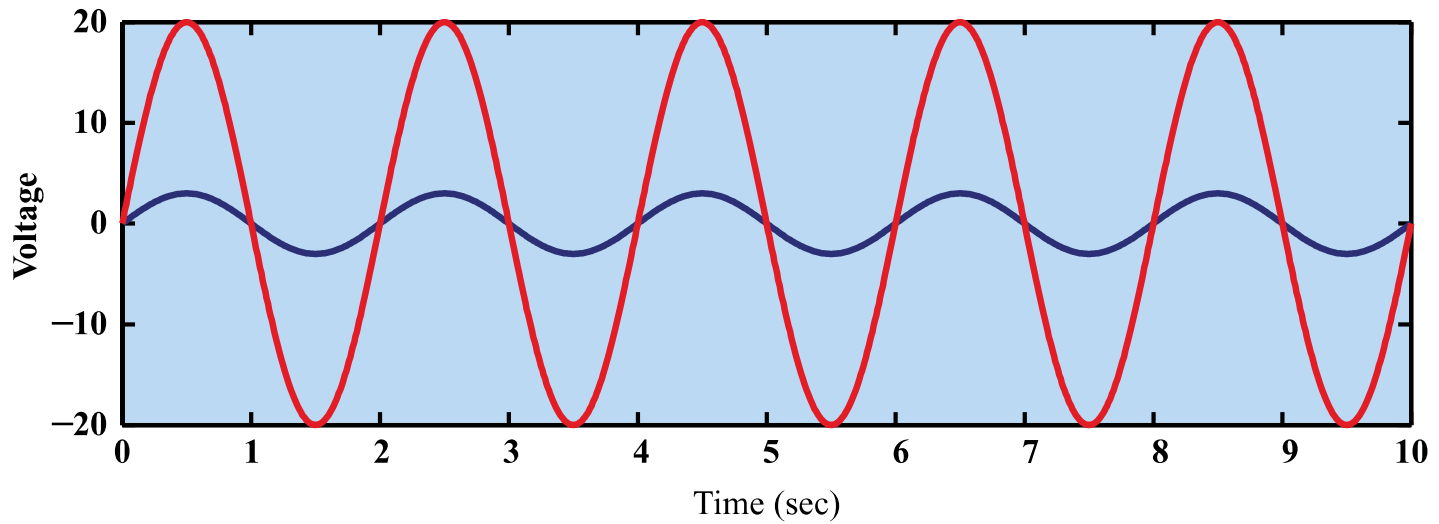
$$V_{out} = KV_{in}$$

- Should have a linear characteristic with slope  $K$  on a  $V_{out}$  vs.  $V_{in}$  curve
- Yet practical amplifiers have limited linear ranges
  - Causing distortion if outside the linear range

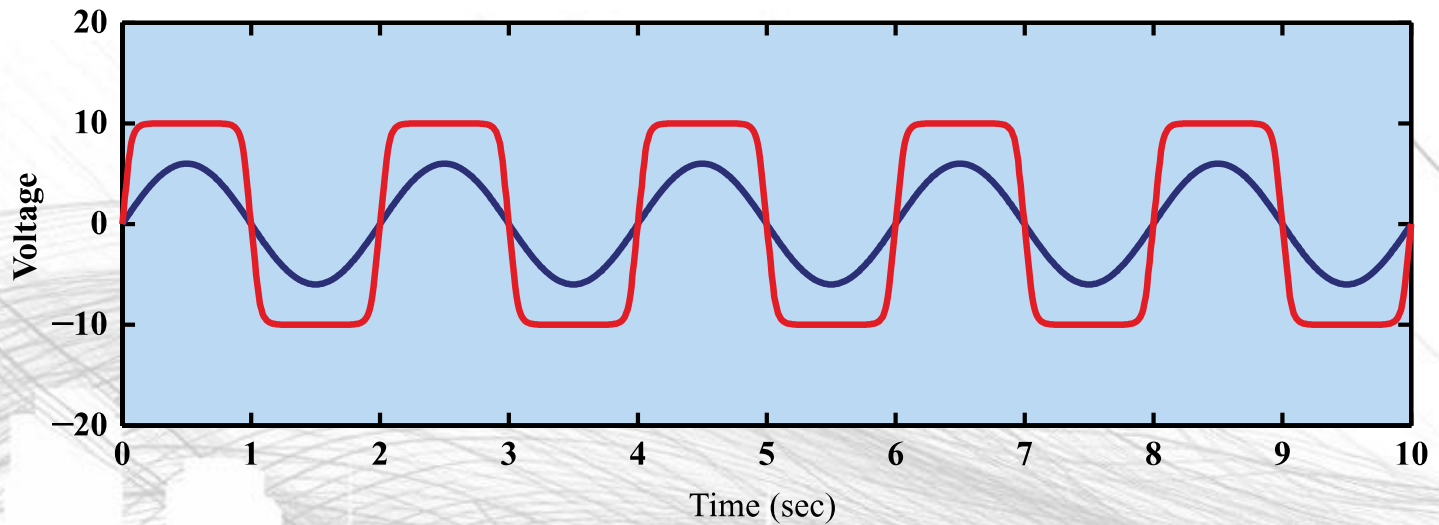


**FIGURE 8.5 IDEAL AND PRACTICAL AMPLIFIER CHARACTERISTICS**





(a) Input to amplifier



(b) Output from amplifier

**FIGURE 8.6 EXAMPLES OF LINEAR AND NONLINEAR AMPLIFIER OUTPUT**



# DIFFICULTIES OF OFDM

- PAPR problem (continued)
  - Expensive amplifiers have wide linear range
- Solutions
  - Could reduce the peak amplitude
    - Called *input backoff*
    - But this would increase the signal to interference plus noise ratio (SINR)
      - Noise and interference would be relatively stronger because signal is weaker
  - Specific PAPR reduction techniques can be used
    - Specialized coding, phase adjustments, clipping, etc.
    - Single-carrier FDMA (SC-FDMA)

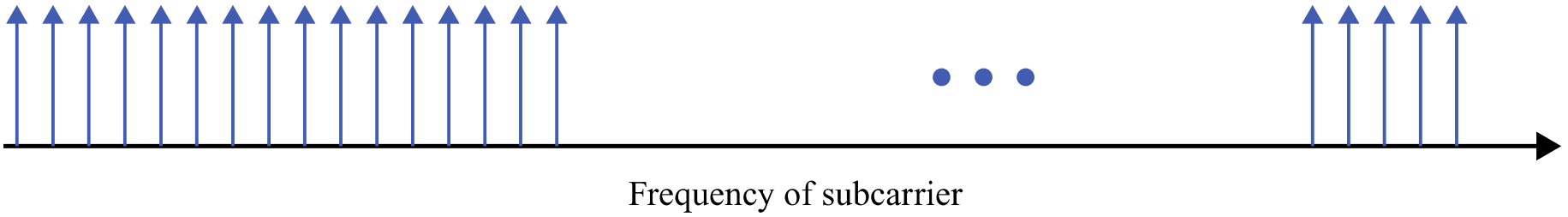


# DIFFICULTIES OF OFDM

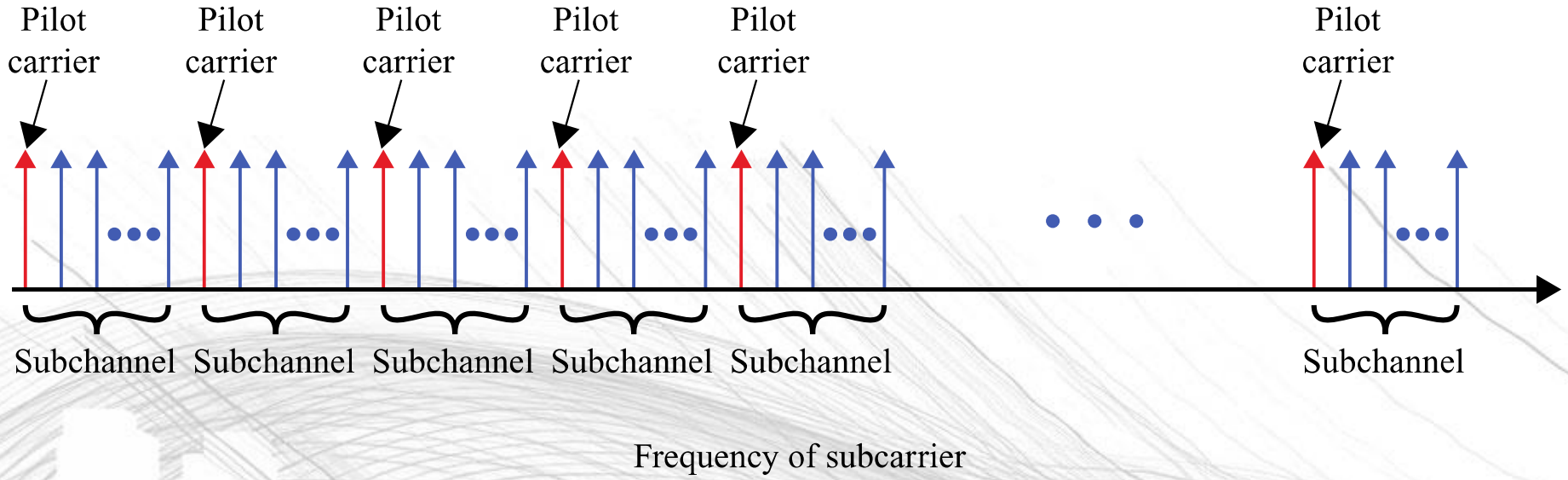
- Intercarrier Interference (ICI)
  - OFDM frequencies are spaced very precisely
  - Channel impairments can corrupt this
  - Cyclic prefix helps reduce ICI
    - But CP time should be limited so as to improve spectral efficiency
    - A certain level of ICI may be tolerated to have smaller CPs
  - Doppler spread, mismatched oscillators, or even one subcarrier can cause ICI
    - Spacing between subcarriers may need to be increased
    - Could also use different pulse shapes, self-interference cancellation, or frequency domain equalizers.

# OFDMA

- Orthogonal Frequency Division Multiple Access (OFDMA) uses OFDM to share the wireless channel
  - Different users can have different slices of time and different groups of subcarriers
  - Subcarriers are allocated in groups
    - Called subchannels or resource blocks
    - Too much computation to allocate every subcarrier separately
- Subchannel allocation
  - Adjacent subcarriers – similar SINR
    - Must measure to find the best subchannel
  - Regularly spaced subcarriers – diverse SINR
  - Randomly space subcarriers – diverse SINR and reduced adjacent-cell interference



**(a) OFDM**



**(b) OFDMA (adjacent subcarriers)**

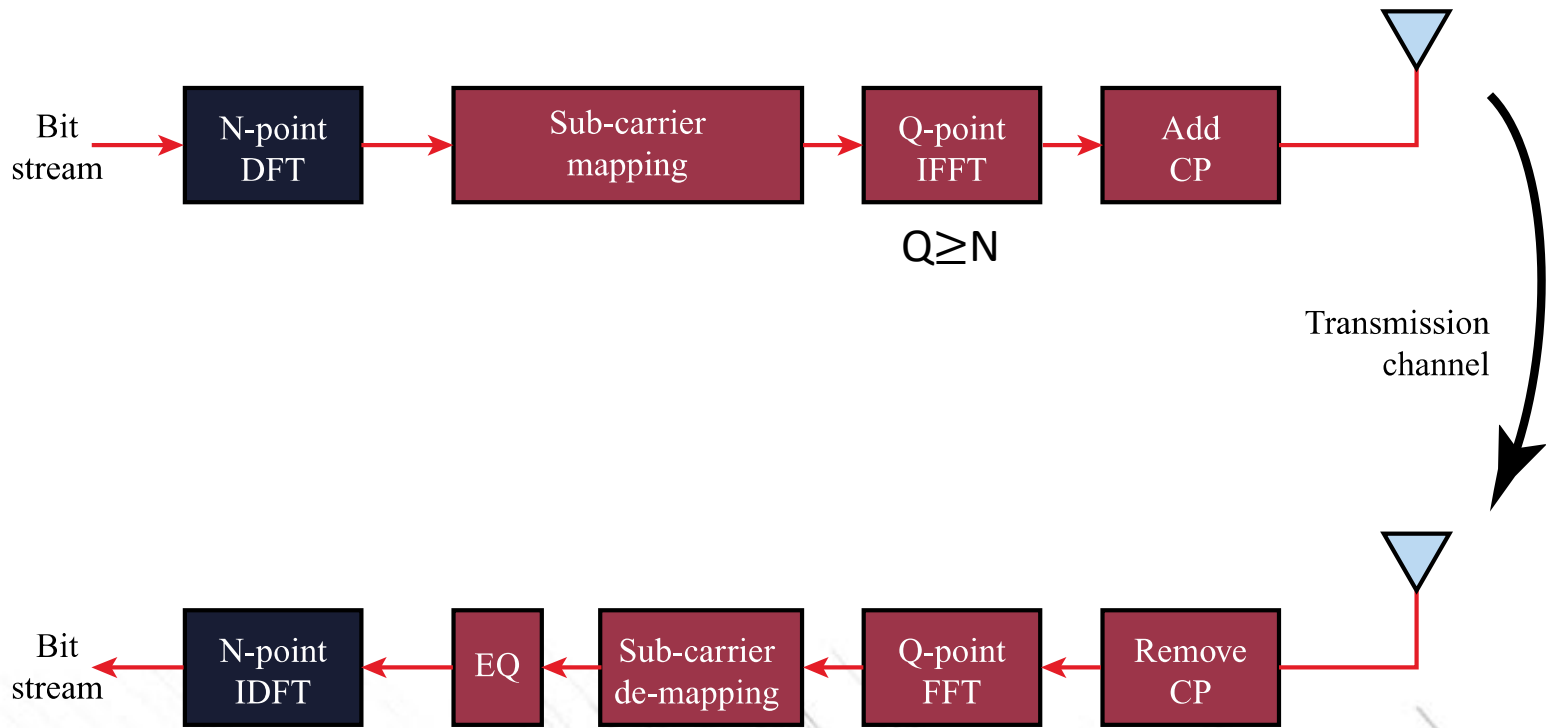
**FIGURE 8.7 OFDM AND OFDMA**

# OPPORTUNISTIC SCHEDULING

- Schedule subchannels and power levels based on
  - Channel conditions
  - Data requirements
- Adjust in a dynamic fashion
  - Use channel variations as an opportunity to schedule the best choice in users
    - Hence the term *opportunistic scheduling*
  - Criteria (maybe more than one used simultaneously)
    - System efficiency – pick users with best throughput
    - Fairness – proportional fairness considers the ratio of users' current rates to the users' average rates to know when a channel is best *for them*
    - Requirements – audio, video
    - Priority – public safety, emergency, or priority customers

# SINGLE-CARRIER FDMA

- SC-FDMA has similar structure and performance to OFDMA
  - But lower PAPR
  - Mobile user benefits – battery life, power efficiency, lower cost
  - Good for uplinks
- Uses extra DFT operation and frequency equalization compared to OFDM
  - DFT prior to IFFT
  - Spreads data symbols over all subcarriers
  - Every data symbol is carried by every subcarrier
- Multiple access is possible
  - Subcarrier groups assigned to different users.
  - User transmits in assigned subcarriers treating other users' subcarriers as nulls.



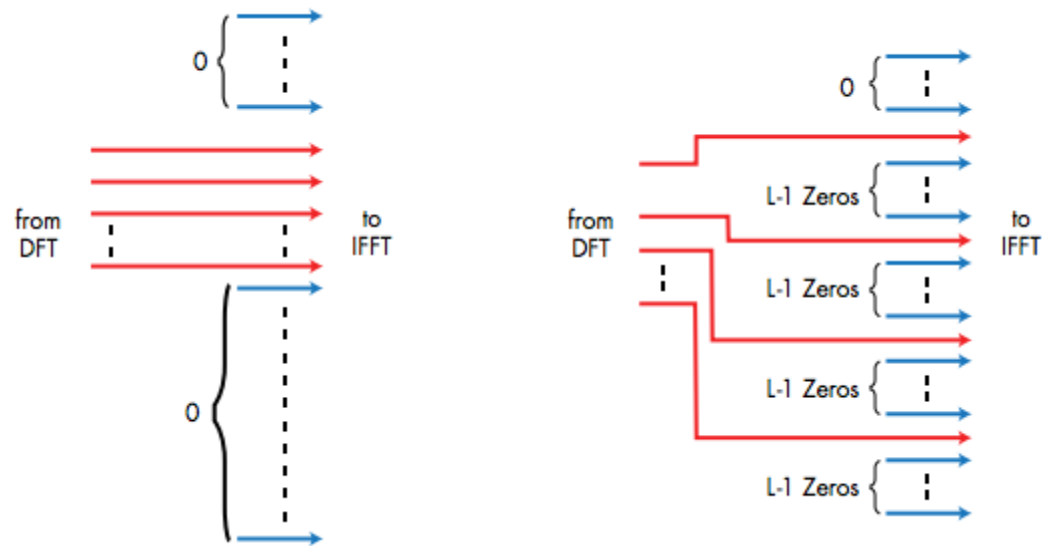
SC-FDMA:  +

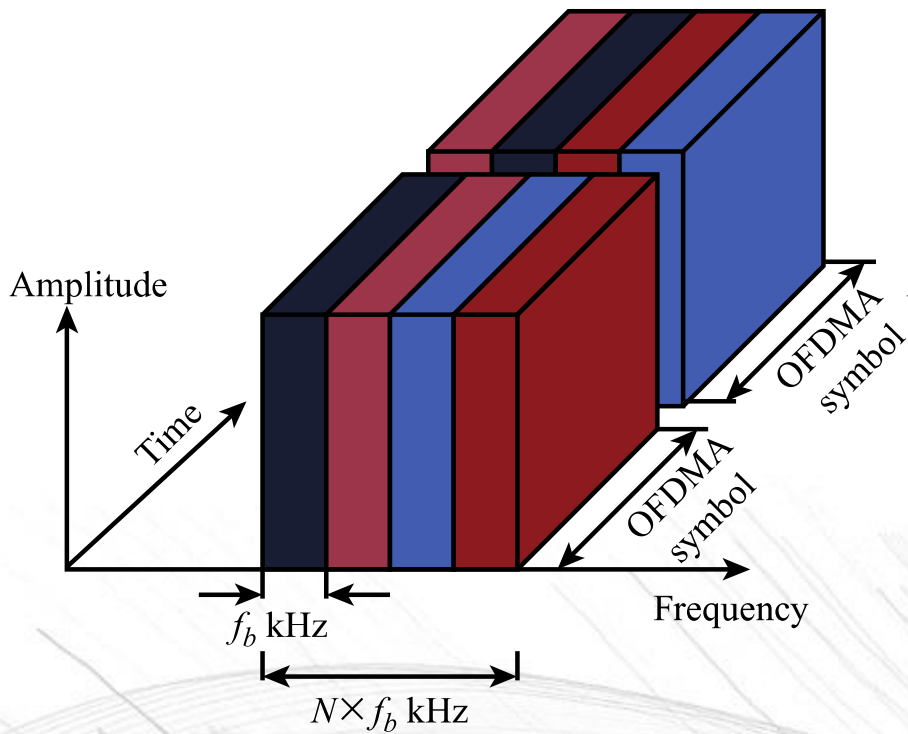
OFDMA:

DFT = discrete Fourier transform  
 IDFT = inverse discrete Fourier transform  
 FFT = fast Fourier transform  
 IFFT = inverse fast Fourier transform  
 EQ = subcarrier equalization  
 CP = cyclic prefix

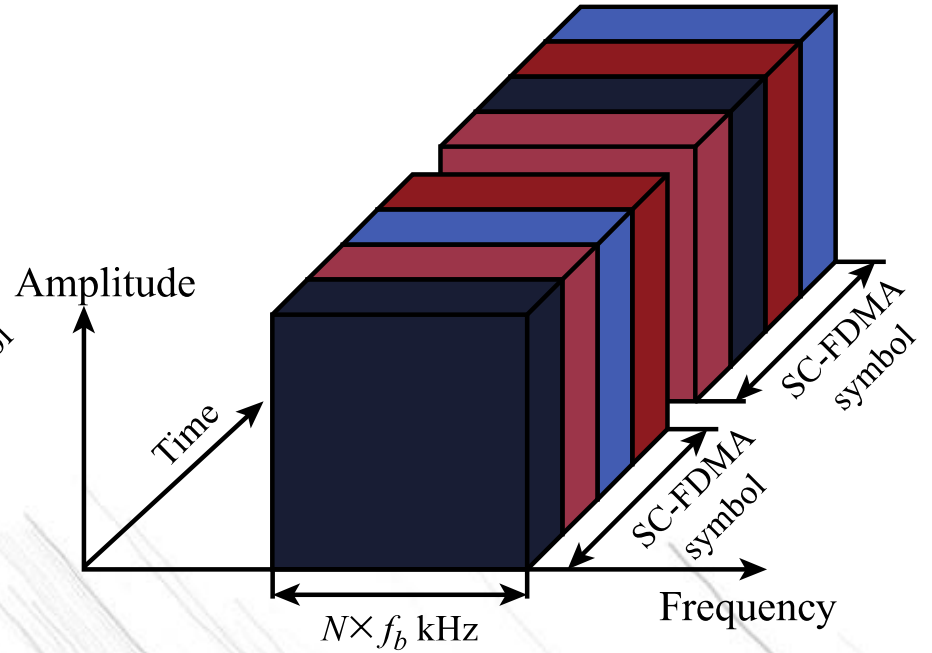
**FIGURE 8.8 SIMPLIFIED BLOCK DIAGRAM OF OFDMA AND SC-FDMA**

# SUBCARRIER MAPPING





(a) OFDMA: Data symbols occupy  $f_b$  kHz for one OFDMA symbol period



(b) SC-FDMA: Data symbols occupy  $N \times f_b$  kHz for  $1/N$  SC-FDMA symbol period

**FIGURE 8.9 EXAMPLE OF OFDMA AND SC-FDMA**